Hall effect in Ce\textsubscript{1-x}Y\textsubscript{x}Pd\textsubscript{3} mixed-valence alloys

A. Fert, P. Pureur,* and A. Hamzic

Laboratoire de Physique des Solides, Université de Paris-Sud, F-91405 Orsay, France

J. P. Kappler

Laboratoire de Magnetisme et de Structure Electronique des Solides,
3 rue de l'Université, F-67084 Strasbourg, France

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Mixed-valence and Kondo lattice systems exhibit large anomalous Hall coefficients with a striking change of sign at low temperature in several systems (CePd\textsubscript{3}, CeCu\textsubscript{6}, . . .). We have studied the Hall effect of Ce\textsubscript{1-x}Y\textsubscript{x}Pd\textsubscript{3}, in which the substitution of small amounts of Y for Ce prevents the development of coherence at low temperature. We find that the Hall coefficient does not change its sign at low temperature and can be well understood in the one-impurity model of Ramakrishnan, Coleman, and Anderson. We infer that the change of sign observed in CePd\textsubscript{3} is an effect of coherence.

Mixed-valence and Kondo rare-earth systems exhibit anomalous Hall coefficients, as has been observed in Ce (Refs. 1 and 2) and Tm (Ref. 3) dilute alloys and in several intermetallic compounds.\textsuperscript{4-9} A striking result is the change of sign of the Hall coefficient in CePd\textsubscript{3},\textsuperscript{5} SmB\textsubscript{6},\textsuperscript{6} CeBe\textsubscript{13},\textsuperscript{5} CeCu\textsubscript{6},\textsuperscript{6,9} and YbCuAl.\textsuperscript{5} A plausible origin of these Hall-effect anomalies is the existence of skew scattering.\textsuperscript{10} An early model\textsuperscript{11} of the Hall effect induced by Kondo Ce impurities was based on the calculation of the skew scattering by a Coqblin-Schrieffer interaction\textsuperscript{12} between conduction electrons and Ce impurities. This model is valid only in the high-temperature limit, i.e., $T >> T_K$. Recently, a more general model has been proposed by Ramakrishnan, Coleman, and Anderson.\textsuperscript{13,14} The expression of the Hall coefficient found by these authors [see Eqs. (4) and (9) in Ref. 13] is written as

$$R_H = R_0^g + g \mu_B |\alpha| \rho \sin(\phi + \delta_2)/\sin\delta_2 ,$$

(1)

with $\phi = -2\delta_2$ in the low-temperature limit ($T << T_K$) and $\phi = -\pi$ in the high-temperature limit. $\delta_2$ is the phase shift associated with the resonance scattering in the $I=3$ channel at low temperature, $\delta_1$ is the phase shift due to additional potential scattering in the $I=2$ channel, $\rho$ is the resistivity, and $|\alpha|$ is proportional to $X(1-\chi T)$, where $X$ is the reduced magnetic susceptibility, i.e., $X = 3\chi/\mu_B^2 J(J+1)$. The change of $\phi$ from $-2\delta_2$ to $-\pi$ as the temperature increases is related to the renormalization of the $f$-level position. Ramakrishnan et al.\textsuperscript{13,14} have proposed to ascribe the change of sign of the Hall effect at low temperature to the change of sign of $\sin(\phi + \delta_2)$ as $\phi$ shifts from $-\pi$ to $-2\delta_2$. However, the model of Ramakrishnan et al.\textsuperscript{13,14} describes the skew scattering by independent Ce impurities and does not take into account the coherence effects occurring at low temperature in mixed-valence and Kondo lattices. Alternatively, it is tempting to ascribe the change of sign of the skew scattering term to the onset of coherence and to the resulting changes in the scattering processes. In CePd\textsubscript{3}, for example, $R_H$ is found to drop in the temperature range where coherence appears (drop of the resistivity). In the same way, in CeCu\textsubscript{6}, the change of sign of $R_H$ seems to be related to coherence effects.\textsuperscript{9} In order to establish if the decrease and the change of sign of $R_H$ in CePd\textsubscript{3} is due to the onset of coherence, we have studied the Hall effect of Ce\textsubscript{1-x}Y\textsubscript{x}Pd\textsubscript{3} alloys with $x=0.0,0.1,0.3$. It is known that the substitution of a few atomic percent of Y for Ce in CePd\textsubscript{3} breaks the coherent state: with only 3 at.\% of Y (i.e., $x=0.03$) the resistivity drop at low temperature disappears almost completely;\textsuperscript{15} for $x=10$ and 30 the resistivity levels off at a very high value in the low-temperature limit,\textsuperscript{16} which is the typical behavior for independent mixed-valence and Kondo impurities.\textsuperscript{15} To probe the role of coherence in the change of sign of $R_H$, we compare the Hall effect of coherent CePd\textsubscript{3} and incoherent Ce\textsubscript{1-x}Y\textsubscript{x}Pd\textsubscript{3}.

Samples of Ce\textsubscript{1-x}Y\textsubscript{x}Pd\textsubscript{3} with $x=0.0,0.1$, and 0.3 were prepared from 99.99% pure metals by arc melting under a pure argon atmosphere. The magnetic and transport properties of samples prepared in this way have been described previously.\textsuperscript{16} The samples for Hall-effect studies were in the form of platelets ($1 \times 3 \times 10$ \text{mm$^3$}) and the measurements were performed by a standard ac technique up to 7 T between 1.2 K and room temperature. We present below our results on the initial Hall coefficient $R_H$.

In Fig. 1 we show $R_H$ vs $T$ for our three samples. Our results for CePd\textsubscript{3} confirm the change of sign at about 20 K already observed by Cattaneo, Häfner, and Wohlleben.\textsuperscript{5} On the contrary, for Ce\textsubscript{0.9}Y\textsubscript{0.1}Pd\textsubscript{3} and Ce\textsubscript{0.9}Y\textsubscript{0.3}Pd\textsubscript{3}, $R_H$ increases monotonically when $T$ is lowered from room temperature to 1.2 K. For these two Ce\textsubscript{1-x}Y\textsubscript{x}Pd\textsubscript{3} alloys the variation of $R_H$ with $T$ fits roughly the variation of $\rho X(1-\chi T)$ calculated from independent measurements of $\rho$ and $X$ (Refs. 16 and 19) and represented by dashed curves in Fig. 1. This rough agreement between the variation of $R_H$ and $\rho X(1-\chi T)$ (Ref. 20) means the Hall effect of our two Ce\textsubscript{1-x}Y\textsubscript{x}Pd\textsubscript{3} alloys is approximately explained by the one-impurity model of Ramakrishnan et al. with temperature-independent values of $\phi$ in Eq. (1) (from the neutron quasielastic width\textsuperscript{21} and the susceptibility data,\textsuperscript{16} the Kondo temperature $T_K$ of our Ce\textsubscript{1-x}Y\textsubscript{x}Pd\textsubscript{3} alloys is in the range 500–1000 K, which is consistent with an approximately constant value of $\phi$ in our experimental range 1–300 K).

Now, if the behavior of $R_H$ for $x=0.1$ and 0.3 is characteristic of incoherent Ce and explained by the one-impurity model of Ramakrishnan et al., we infer that the behavior of $R_H$ in CePd\textsubscript{3}, with a drop below 100 K and a change of sign at about 20 K, has to be ascribed to the onset of coherence. It has been suggested to one of us (A.F.) by Coleman that the effect of coherence might be described by introducing a crystal-field splitting in the coherent state and the resulting
new phase shifts in Eq. (1). However, comparing the susceptibility and the Wilson ratio of CePd$_3$ and Ce$_{1-x}$Y$_x$Pd$_3$ (Ref. 16) hardly supports the idea of different crystal-field splittings in the coherent and incoherent states. Rather we believe that a specific treatment of the scattering processes in the coherent state is needed to explain the Hall effect. In the presence of coherence the electrons are scattered only by the nonperiodic part of the potential, i.e., by fluctuations about the coherent state. A similar situation occurs in the Hall effect of ferromagnets such as Gd, Tb, Dy, . . . . In the paramagnetic state the anomalous Hall effect is due to independent orbital exchange terms, $V'_{\text{scatt}} \approx -(1-\chi)$, whereas, in the ferromagnetic state, the scattering is due to fluctuations about the ferromagnetic state, $V'_{\text{scatt}} \approx 1 - (J_i - \langle J_i \rangle)$, and this even leads, in some cases, to a change of sign of the anomalous Hall effect between $T_c$ and 0 K.22 Of course, the problem of the scattering by fluctuations about the coherent state is likely much more complex. In addition, the change of the band structure and Fermi surface at the onset of coherence could also affect the scattering processes significantly.

In conclusion, our results on Ce$_{1-x}$Y$_x$Pd$_3$ alloys show that the change of sign of the Hall effect in CePd$_3$ is a coherence effect and disappears when Y impurities prevent the development of coherence. For the incoherent Ce$_{1-x}$Y$_x$Pd$_3$ alloys, the Hall coefficient fits the predictions of the independent impurity model of Ramakrishnan et al.13,14 The relation between the change of sign of the Hall coefficient and the onset of coherence seems to have also been observed in other systems and poses an interesting problem.

$^{1}$Permanent address: University of Rio Grande do Sul, Porto Alegre, Brasil.
$^{2}$Permanent address: Institute of Physics of the University, 41001 Zagreb, Yugoslavia.
$^{11}$Permanent address: University of Rio Grande do Sul, Porto Alegre, Brasil.
$^{18}$In fact, our CePd$_3$ sample is a Ce$_{29}$Pd$_{71}$ alloy for which the coherence effects are slightly stronger than in Ce$_{26}$Pd$_{74}$; see M. J. Besnus, J. P. Kappler, and A. Meyer, J. Phys. F 13, 597 (1983).
$^{19}$For Ce$_{0.9}$Y$_{0.1}$Pd$_3$ and Ce$_{0.7}$Y$_{0.3}$Pd$_3$, 1-\chi departs little from 1 in our temperature range, so that the variation of $\rho x(1-\chi)$ is essentially that of $\rho x$.
$^{20}$The ordinary Hall coefficient $R_H^0$ is approximately known from data on YPd$_3$, see Ref. 5. It is relatively small and, in first approximation, can be neglected in Eq. (1).