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Signatures of the Berezinskii-Kosterlitz-Thouless transition in the location of the zeros of the canonical partition function for the 2D XY-model,

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In this work we show how one can use the zeros of the canonical partition function, the Fisher zeros, to unambiguously characterize a transition as being in the Berezinskii-Kosterlitz-Thouless (*BKT*) class of universality.

A “fruit fly” model of the *BKT* transition is the classical two-dimensional XY-model on a square lattice, defined by

$$\mathcal{H} = -J \sum_{\langle i,j \rangle} (S_i^x S_j^x + S_i^y S_j^y). \quad (1)$$

The sum runs over the nearest neighbors, J stands for the exchange coupling constant and S_i^α stands for the component $\alpha = (x, y, z)$ of the i^{th} spin.

We obtained the Fisher’s zeros map via recent Monte Carlo simulations techniques (Replica Exchange Wang-Landau) capable of sampling the entire configuration space efficiently in a single simulation and powerful matrix diagonalization procedures.

We found that in a *BKT* transition the internal border of the zeros map behave in such a way that for $T \leq T_{BKT}$ it coalesces into the real positive axis in the thermodynamic limit, indicating the existence of a line of critical points in this region, as should be expected, and in contrast to what happens for a continuous or discontinuous phase transition, where a single leading zero touches the positive real axis. This behavior is therefore the signature of the *BKT* transition. The inflection point of the zeros map was successfully used to obtain the *BKT* temperature, $T_{BKT} = 0.704(3)$, in excellent accordance with the literature.

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