

# VERY LOW MASS STELLAR AND SUBSTELLAR COMPANIONS TO SOLAR-LIKE STARS FROM MARVELS. I. A LOW-MASS RATIO STELLAR COMPANION TO TYC 4110-01037-1 IN A 79 DAY ORBIT

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## ABSTRACT

TYC 4110-01037-1 has a low-mass stellar companion, whose small mass ratio and short orbital period are atypical among binary systems with solar-like ( $T_{\text{eff}} \lesssim 6000$  K) primary stars. Our analysis of TYC 4110-01037-1 reveals it to be a moderately aged ( $\lesssim 5$  Gyr) solar-like star having a mass of  $1.07 \pm 0.08 M_{\odot}$  and radius of  $0.99 \pm 0.18 R_{\odot}$ . We analyze 32 radial velocity (RV) measurements from the SDSS-III MARVELS survey as well as 6 supporting RV measurements from the SARG spectrograph on the 3.6 m Telescopio Nazionale Galileo telescope obtained over a period of  $\sim 2$  years. The best Keplerian orbital fit parameters were found to have a period of  $78.994 \pm 0.012$  days, an eccentricity of  $0.1095 \pm 0.0023$ , and a semi-amplitude of  $4199 \pm 11 \text{ m s}^{-1}$ . We determine the minimum companion mass (if  $\sin i = 1$ ) to be  $97.7 \pm 5.8 M_{\text{Jup}}$ . The system's companion to host star mass ratio,  $\geq 0.087 \pm 0.003$ , places it at the lowest end of observed values for short period stellar companions to solar-like ( $T_{\text{eff}} \lesssim 6000$  K) stars. One possible way to create such a system would be if a triple-component stellar multiple broke up into a short period, low  $q$  binary during the cluster dispersal phase of its lifetime. A candidate tertiary body has been identified in the system via single-epoch, high contrast imagery. If this object is confirmed to be comoving, we estimate it would be a dM4 star. We present these results in the context of our larger-scale effort to constrain the statistics of low-mass stellar and brown dwarf companions to FGK-type stars via the MARVELS survey.

*Key words:* binaries: general – stars: individual (TYC 4110-01037-1) – stars: low mass

*Online-only material:* color figures

## 1. INTRODUCTION

Observations of the mass distribution of substellar and low-mass stars as a function of orbital separation, using a variety of techniques, provide key constraints which influence our understanding of the process of planetary and star formation (Burgasser et al. 2007; Stamatellos & Whitworth 2009; Kraus et al. 2011; Sahlmann et al. 2011). Early results from the Kepler transit search program, which is sensitive to short to moderate period companions, show the size distribution of candidate

companions increases toward smaller planets, reaching a maximum at a few  $R_{\oplus}$  (Borucki et al. 2011a, 2011b). Numerous large radial velocity (RV) surveys are constraining the prevalence of Jovian-mass giant planets at close and intermediate orbital separations (e.g., California & Carnegie teams, Marcy & Butler 2000; AAPS, Tinney et al. 2001; CORALIE, Udry et al. 2000; HARPS, Mayor et al. 2004) and the prevalence of brown dwarf (BD) and very low mass stellar companions at close and intermediate separations (Marcy & Butler 2000; Mayor et al. 2001; Vogt et al. 2002; Patel et al. 2007; Lee et al. 2011). At much

larger orbital separations, high contrast imaging surveys inform our understanding of the mass distribution of planets (Kalas et al. 2008; Marois et al. 2008, 2010; Lagrange et al. 2010) and BDs (Thalmann et al. 2009; Biller et al. 2010; Janson et al. 2011; Wahhaj et al. 2011), while the mass distribution of very low mass stellar companions has been explored by high contrast imaging (Kraus et al. 2011), spectroscopic (Duquennoy & Mayor 1991), and interferometric (Raghavan et al. 2010) studies.

Many of the results from these surveys have found interesting, and at times conflicting, trends motivating subsequent programs to investigate their origin. In the BD regime, a deficit of short period ( $a \leq 5$  AU) companions to solar-type primary stars has long been designated the apparent “brown dwarf desert” (Marcy & Butler 2000). Investigations of the BD frequency at larger orbital separations (e.g., Gizis et al. 2001; Metchev & Hillenbrand 2004; McCarthy & Zuckerman 2004; Carson et al. 2005; Metchev & Hillenbrand 2009; Kraus et al. 2011) have led to conflicting assertions as to whether the BD desert extends to larger orbital separations. Multiplicity studies of low-mass stellar companions to solar-like stars have found evidence of a unimodal period distribution with peak periods ranging from  $\sim 180$  years (Duquennoy & Mayor 1991) to  $\sim 300$  years (Raghavan et al. 2010). Interestingly, recent work by Metchev & Hillenbrand (2009) has presented tentative evidence that the companion mass function of BD and low-mass stellar companions around solar-like stars could be represented by a universal function.

At the short-period ( $P < 100$  days) tail of solar-like ( $T_{\text{eff}} \lesssim 6000$  K) multiplicity investigations, many studies have reported a paucity of confirmed low-mass stellar or BD companions with mass ratios ( $q \equiv M_c/M_*$ )  $< 0.2$  (see, e.g., Pont et al. 2005; Bouchy et al. 2011), leading Raghavan et al. (2010) to suggest that short period companions to solar-like stars prefer higher mass ratios, although there is disagreement in the literature regarding this trend (see, e.g., Halbwachs et al. 2003). Burgasser et al. (2007) suggest that the short-period BD desert seems to extend into the M dwarf regime. Raghavan et al. (2010) also note that the majority of the companions surrounding solar-like stars with periods  $< 100$  days are triple systems, and thus potentially indicative that such systems experienced orbital migration (Bate et al. 2002). Short-period low-mass ratio binaries are much more commonly observed around slightly more massive F-type stars (Bouchy et al. 2005; Pont et al. 2006; Beatty et al. 2007; Bouchy et al. 2011). Bouchy et al. (2011) have suggested that low  $q$  companions can form at or migrate to short orbital periods around a wide range of stellar primary masses, but suggest that they may not survive around G dwarfs and lesser mass primary stars.

The Multi-object APO Radial Velocity Exoplanet Large-area Survey (MARVELS), one of the three surveys being executed during the Sloan Digital Sky Survey (SDSS) III (Eisenstein et al. 2011), is a four-year program which is monitoring the radial velocities of  $\sim 3300$   $V = 7.6$ – $12$  FGK-type dwarfs and subgiants. As described in Lee et al. (2011), the target selection strategy attempts to impose minimal and well-understood biases on targets’ ages and metallicities; hence, the survey provides an ideal, statistically robust means to explore the mass distribution of substellar and very low mass star companions over orbital periods of  $\leq 2$  years from a relatively low-biased target sample. In anticipation of a statistical analysis of global trends in the population of BDs and low-mass binary companions identified by the survey, we are performing detailed and careful characterization of the fundamental parameters of these companions and their host stars (see, e.g., Fleming et al.

2012, in preparation, discussion of MARVELS-2b). The first paper in this series was Lee et al. (2011), which presented an analysis of a short period BD surrounding the F9 star TYC 1240-00945-1. Analogous detailed characterization of individual systems has been shown to be particularly important in refining the radii of Kepler candidate planet-candidates to be more Earth-like than assumed (Muirhead et al. 2011). The advantages of meta-analyzing such well-characterized systems is also demonstrated in Bouchy et al. (2011), who were able to begin to explore the mass–radius relationship from the planetary to BD to very low mass star regimes as well as the mass ratio of companions as a function of primary mass.

In this paper, we present a detailed analysis of the fundamental properties of the solar-like star TYC 4110-01037-1 (hereafter TYC 4110) and report the discovery of a very low mass stellar companion associated with the system. In Section 2, we describe the spectroscopic and photometric data which were used for this analysis. We determine accurate fundamental stellar parameters for the star in Section 3 and describe the basic properties of the very low mass stellar companion in Section 4. We also discuss the detection of a candidate tertiary companion system in Section 4. Finally, we discuss the implications of these results in Section 5.

## 2. OBSERVATIONS AND DATA REDUCTION

### 2.1. SDSS-III Radial Velocity Data

Our primary RV observations of TYC 4110 were obtained during the first two years of the SDSS-III MARVELS survey, which uses a dispersed fixed-delay interferometer (Ge et al. 2009) on the SDSS 2.5 m telescope (Gunn et al. 2006). A total of 32 observations were obtained over the course of  $\sim 2$  years. Each 50 minute observation yielded two fringing spectra (aka. “beams”) from the interferometer spanning the wavelength regime  $\sim 500$ – $570$  nm with  $R \sim 12,000$ . Lee et al. (2011) describe the basic data reduction and analysis leading to the production of differential RVs for each beam of the interferometer. We combined these beams for each observation set using a weighted mean. As described in Fleming et al. (2010), we scaled up the RV errors by a “quality factor” ( $Q = 5.67$  for TYC 4110) based on the rms errors of the other stars observed on the same SDSS-III plate as TYC 4110.

A summary of the relative amplitude RV measurements obtained for TYC 4110 with MARVELS is presented in Table 1.

### 2.2. TNG Follow-up Radial Velocity Data

Supporting RV observations were obtained with the 3.6 m Telescopio Nazionale Galileo (TNG) using its SARG spectrograph (Gratton et al. 2001). The  $0'.8 \times 5'.3$  slit provided  $R \sim 57,000$  spectroscopy between 462–792 nm. We obtained six spectra with an iodine cell (IC), to provide high precision radial velocities (Table 1), and one without the IC to serve as a stellar template. The data were reduced using standard IRAF routines and RVs were measured using the IC technique (Marcy & Butler 2000). Each of 21 SARG spectral orders between 504 and 611 nm were divided in 10 pieces, and RV calculations were derived from each of the 210 resulting pieces. Based on a goodness-of-fit indicator, the best 158 (75%) pieces were selected. Following a  $2\sigma$  clip, the remaining RV measurements were combined with a weighted average to produce the RV measurements quoted in Table 1.

**Table 1**  
Summary of Observed Radial Velocities

HJD	Instrument	RV (km s <sup>-1</sup> )	$\sigma_{RV}$ (km s <sup>-1</sup> )
2454811.815473	M	-2.869	0.053
2454812.936774	M	-2.386	0.049
2454816.915562	M	-0.841	0.060
2454840.865816	M	3.859	0.046
2454842.900506	M	3.614	0.093
2454843.814123	M	3.496	0.057
2454844.776592	M	3.342	0.045
2454845.779836	M	3.153	0.049
2454867.724621	M	-2.229	0.072
2454868.791455	M	-2.527	0.048
2454869.785190	M	-2.786	0.070
2454901.671359	M	1.393	0.068
2455105.974063	M	-2.454	0.046
2455135.969729	M	0.417	0.039
2455141.825627	M	2.508	0.045
2455142.892315	M	2.744	0.060
2455143.904775	M	2.978	0.058
2455144.904270	M	3.187	0.042
2455161.844226	M	3.115	0.047
2455199.808399	M	-4.240	0.059
2455201.786093	M	-4.002	0.040
2455202.835898	M	-3.854	0.042
2455280.657591	M	-4.064	0.046
2455287.644203	M	-2.150	0.052
2455463.908559	M	3.816	0.073
2455470.923509	M	4.025	0.042
2455472.000492	M	3.942	0.047
2455498.003488	M	-1.744	0.066
2455500.992667	M	-2.521	0.059
2455516.486551	S	-4.209	0.061
2455516.579785	S	-4.118	0.033
2455542.731058	M	3.798	0.049
2455545.783002	M	4.117	0.053
2455553.524971	S	3.677	0.036
2455556.930997	M	3.175	0.076
2455580.495813	S	-2.702	0.034
2455666.464340	S	-4.051	0.037
2455698.384891	S	3.375	0.041

**Notes.** A summary of relative radial velocities obtained with the MARVELS (M) and SARG (S) spectrographs. The quoted  $\sigma_{RV}$  errors for the MARVELS data were first uniformly scaled by a “quality factor”  $Q = 5.67$  (see Fleming et al. 2010), based on the rms of the other stars observed on the same SDSS-III plate. As described in Section 4, the errors of the MARVELS and SARG data were then re-scaled to force our RV fits to have  $P(\chi^2) = 0.5$ , in an iterative manner. Note that zero point offsets have been applied to the RVs compiled in column 3 to force the RVs to vary about 0 m s<sup>-1</sup>.

### 2.3. APO Spectroscopic Data

Two  $R \sim 31,500$  optical ( $\sim 3600\text{--}10000 \text{ \AA}$ ) spectra of TYC 4110 were obtained on UT 2010 September 29 (HJD 2455468) with the Apache Point Observatory 3.5 m telescope and ARC Echelle Spectrograph (ARCES; Wang et al. 2003) to enable accurate characterization of stellar fundamental parameters. The two spectra were obtained using the default  $1''.6 \times 3''.2$  slit and an exposure time of 1200 s. A ThAr lamp exposure was obtained between these integrations to facilitate accurate wavelength calibration. The data were processed using standard IRAF techniques. Following heliocentric velocity corrections, each order was continuum normalized, and the resultant continuum normalized data from each observation were averaged. The final spectrum yielded a signal-to-noise ratio (S/N) of  $\sim 175$  at  $\sim 6500 \text{ \AA}$ .

**Table 2**  
Stellar Properties of TYC 4110-01037-1

Parameter	Value	Uncertainty	Note
$\alpha$ (2000)	06 54 12.3	...	Hog et al. (1998)
$\delta$ (2000)	+60 21 31.4	...	Hog et al. (1998)
NUV	15.715 mag	0.016	GALEX (Morrissey et al. 2007)
$B$	11.159 mag	0.018	This work (HAO)
$V$	10.521 mag	0.019	This work (HAO)
$I_c$	9.788 mag	0.037	This work (HAO)
$J$	9.347 mag	0.023	Cutri et al. (2003)
$H$	9.069 mag	0.210	Cutri et al. (2003)
$K_s$	9.004 mag	0.020	Cutri et al. (2003)
WISE1 ( $3.4 \mu\text{m}$ )	8.932 mag	0.024	...
WISE2 ( $4.6 \mu\text{m}$ )	8.970 mag	0.022	...
WISE3 ( $12 \mu\text{m}$ )	8.934 mag	0.030	...
WISE4 ( $22 \mu\text{m}$ )	8.662 mag	0.344	...
$A_V$	0.16	0.04	This work
$d$	125.1 pc	4.6	This work
$T_{\text{eff}}$	5879 K	29	This work
$\log g$ [cgs]	4.48	0.15	This work
[Fe/H]	-0.01	0.05	This work
$v_{\text{micro}}$	0.94 km s <sup>-1</sup>	0.04	This work
$M_*$	1.07 $M_{\odot}$	0.08	This work
$R_*$	0.99 $R_{\odot}$	0.18	This work
$v_{\text{systemic}}$	25.9 km s <sup>-1</sup>	0.2	...
$v_{\text{rot}} \sin i$	$\lesssim 3$ km s <sup>-1</sup>	...	...

**Note.** A summary of some of the basic observational properties of TYC 4110-01037-1.

### 2.4. HAO Photometric Data

We obtained absolute photometry of TYC 4110 using the Hereford Arizona Observatory (HAO), a private facility in Southern Arizona (observatory code G95 in the IAU Minor Planet Center). HAO employs a 14 inch Meade LX200GPS telescope equipped with a SBIG ST-10XME CCD. Observations in  $B$ ,  $V$ , and  $I_c$  filters were made on 2011 January 15 and 2011 February 10. A total of 22 Landolt standard stars and 9 secondary standards based on Landolt star fields SA98 and SA114 (Landolt 1992) were observed at several airmass values similar to the airmass for TYC 4110. The target’s magnitude was calculated by

$$M_f = M_{f_0} - 2.5 \log_{10}(F_f/g) - (K'_f \cdot m) + (S_f \cdot C), \quad (1)$$

where  $M_f$  is the magnitude for each filter  $f$ ,  $M_{f_0}$  is a constant determined from the standard stars,  $F_f$  is star flux using a large photometry aperture,  $g$  is exposure time,  $K'_f$  is zenith extinction coefficient for each filter,  $m$  is air mass,  $S_f$  is the star color sensitivity (determined from the standard stars), and  $C$  is star color ( $B-V$ ). Solutions for ( $B-V$ ) were obtained by iterating  $V$  and  $B$  magnitudes from initial values 2–3 times. The resultant absolute photometry for TYC 4110 is summarized in Table 2.

### 2.5. SuperWASP Photometric Data

We analyzed five epochs of broadband optical photometry (400–700 nm) of TYC 4110, obtained between 2006 April 7 and 2008 April 14, from the SuperWASP public archive (Butters et al. 2010). Aperture photometry of the 160 individual observations available in the archive, each taken with a 30 s integration time, was computed via the SuperWASP pipeline. Further details about the observational design and data reduction pipeline for SuperWASP can be found in Pollacco et al. (2006). We find the SuperWASP photometry exhibits no statistically significant

evidence of variability (error-weighted rms  $\sim 0.675\%$ ) over the timescales sampled by these data. For example, a linear fit to the entire data set yields negligible variation in flux with a best-fit slope of  $0.040\% \pm 0.030\% \text{ day}^{-1}$ . We also detect no evidence of a transit. We do caution however that the sampling of these data is sparse.

### 3. TYC 4110-01037-1: THE STAR

#### 3.1. Fundamental Stellar Properties

We analyzed moderate resolution spectroscopic data from the ARCES spectrograph using two separate analysis techniques to extract fundamental stellar parameters for TYC 4110. We refer to these different pipeline results as the “IAC” (Instituto de Astrofísica de Canarias) and “BPG” (Brazilian Participation Group) results, as described below.

##### 3.1.1. “IAC” Analysis

We derive equivalent widths (EWs) of Fe I and Fe II lines with the code ARES (Sousa et al. 2007), using an initial line list with 263 Fe I and 36 Fe II lines given in Sousa et al. (2008) and use the rules in Sousa et al. (2008) to modify the *rej*t parameter in ARES according to the S/N of each spectrum. In addition, we set the ARES parameters *smoother* = 4, *space* = 3, and *miniline* = 2. The parameter *lineresol* was modified according to the resolving power of each spectrum.

The stellar atmospheric parameters were computed using the code STEPAR (Taberner et al. 2012). This code employs the 2002 version of the MOOG code (Snedden 1973), and a grid of Kurucz ATLAS9 plane-parallel model atmospheres (Kurucz 1993). STEPAR iterates until the slopes of  $A(\text{Fe I})$  versus  $\chi$  and  $A(\text{Fe I})$  versus  $\log(\text{EW}\lambda^{-1})$  are equal to zero, while imposing the ionization equilibrium condition  $A(\text{Fe I}) = A(\text{Fe II})$ . A  $2\sigma$  rejection of the EWs of Fe I and Fe II lines is performed after a first determination of the stellar parameters, and then the STEPAR program is re-run without the rejected lines (see Taberner et al. 2012 for further details).

For the ARCES spectrum of TYC 4110, 198 Fe I lines and 24 Fe II lines remain after clipping. These are used to derive  $T_{\text{eff}} = 5879 \pm 25 \text{ K}$ ,  $\log(g) = 4.53 \pm 0.18$ ,  $[\text{Fe}/\text{H}] = -0.02 \pm 0.05$ , and  $v_{\text{micro}} = 0.932 \pm 0.038 \text{ km s}^{-1}$ .

Internal uncertainties were also derived for each stellar parameter. The uncertainty of  $v_{\text{micro}}$  was obtained by varying this parameter until the slope of the linear regression of  $A(\text{Fe I})$  versus  $\log(\text{EW}\lambda^{-1})$  was equal to its standard deviation. The uncertainty of  $T_{\text{eff}}$  was determined by changing this parameter until the slope of the linear regression of  $A(\text{Fe I})$  versus  $\chi$  was equal to its standard deviation. The uncertainty of  $v_{\text{micro}}$  was also taken into account when calculating the uncertainty of  $T_{\text{eff}}$ . The uncertainty of  $\log(g)$  was obtained by varying this parameter until the difference between the mean abundances from Fe I and Fe II were equal to the standard deviation of the latter. The contributions from  $T_{\text{eff}}$  and  $v_{\text{micro}}$  were included. Finally, the uncertainty of  $[\text{Fe}/\text{H}]$  is a combination of the standard deviation of the Fe I abundance and the variations caused by the errors in  $T_{\text{eff}}$ ,  $\log(g)$ , and  $\xi_t$ , all added in quadrature.

##### 3.1.2. “BPG” Analysis

We assume LTE and use the 2002 version of MOOG (Snedden 1973), along with the one-dimensional plane-parallel model atmospheres interpolated from the ODFNEW grid of ATLAS9 models (Castelli & Kurucz 2004). Initially, a list of  $\sim 150$

isolated and moderately strong (i.e.,  $5 < \text{EW} < 120 \text{ mÅ}$ ) Fe I and Fe II lines was compiled using the Solar Flux Atlas (Kurucz et al. 1984), the Utrecht spectral line compilation (Moore et al. 1966), and a Ganymede ARCES spectrum with S/N = 400. The values for the central wavelengths and line excitation potentials were taken from the Vienna Atomic Line Database (Kupka et al. 1999). We also multiplied the van der Waals damping parameter “C6” by a factor of two, following Holweger et al. (1991).

The EWs of these lines were automatically measured in the solar spectrum from fits of Gaussian profiles using the task *bplot* in IRAF. The quality of the measurements was checked by performing two tests. First, since the line depth is expected to be a linear function of the reduced EW ( $\text{EW}\lambda^{-1}$ ) for non-saturated lines, we eliminated lines that did not follow a linear relation, using a  $2\sigma$  clipping. The second test is based on the fact that the shapes of the lines are essentially determined by the instrumental profile at the APO resolution ( $\sim 31,500$ ). Since the resolution is approximately constant over the entire spectrum, we expect the quantity  $\text{FWHM}\lambda^{-1}$  to be approximately constant for lines of the same species. We therefore perform a linear fit to this relation and eliminate lines that exhibit  $2\sigma$  deviations.

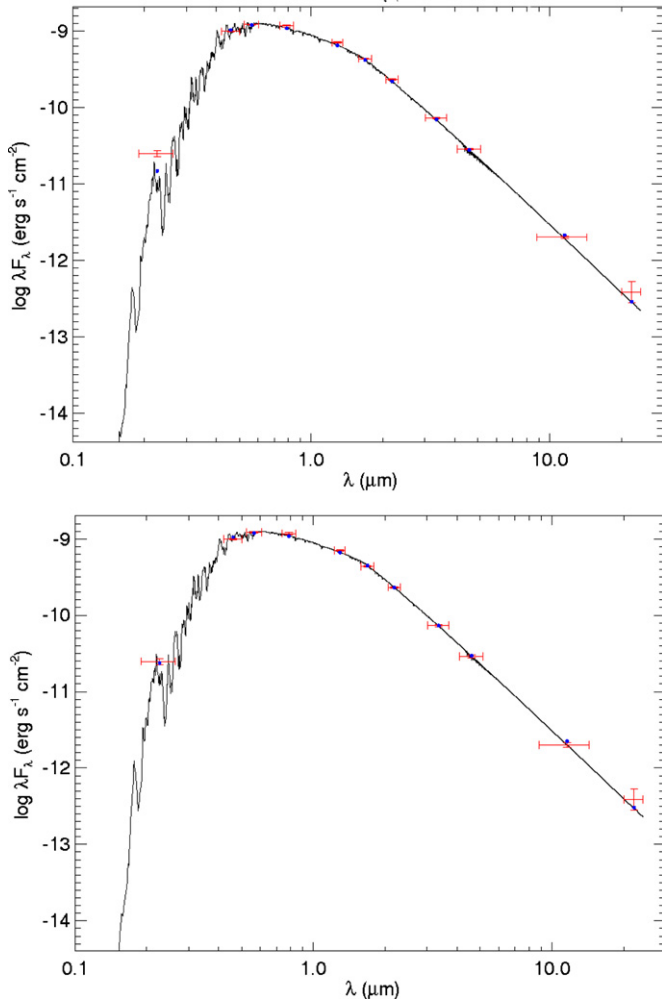
After these tests, the final solar line list contained 91 Fe I and 11 Fe II lines. Solar *gf* values were derived for all these lines using a solar model atmosphere with the following parameters:  $T_{\text{eff}} = 5777 \text{ K}$ ,  $\log(g) = 4.44$ ,  $[\text{Fe}/\text{H}] = 0.0$ , and  $v_{\text{micro}} = 1.0 \text{ km s}^{-1}$ . The adopted solar abundance for iron is  $A(\text{Fe}) = 7.50$  (Asplund et al. 2009).

EWs for 102 Fe lines were measured in the TYC 4110 APO spectrum and checked with the tests described above.  $T_{\text{eff}}$  and  $v_{\text{micro}}$  were iterated until zero slopes were found in the plots of  $A(\text{Fe I})$  versus  $\chi$  and  $\log(\text{EW}\lambda^{-1})$ , respectively; i.e., until the individual Fe I line abundances were independent of excitation potential and reduced EWs. The surface gravity was iterated until  $A(\text{Fe I}) = A(\text{Fe II})$ , i.e., until the same average abundances were given by Fe I and Fe II lines. At the end of this iterative process, a consistent set of atmospheric parameters ( $T_{\text{eff}}$ ,  $\log(g)$ ,  $[\text{Fe}/\text{H}]$ , and  $v_{\text{micro}}$ ) was obtained for the star. Note that the metallicity is simply given by  $[\text{Fe}/\text{H}] = A(\text{Fe}) - 7.50$ , where 7.50 is the solar iron abundance taken from Asplund et al. (2009). At this point, any lines with abundances that deviated more than  $2\sigma$  from the average were removed and the above iteration was repeated until convergence was achieved.

We derive  $T_{\text{eff}} = 5878 \pm 49 \text{ K}$ ,  $\log(g) = 4.43 \pm 0.17$ ,  $[\text{Fe}/\text{H}] = 0.00 \pm 0.06$ , and  $v_{\text{micro}} = 1.00 \pm 0.08 \text{ km s}^{-1}$  based on the ARCES spectrum. The final line list after rejections contained 60 Fe I and 8 Fe II lines. The internal uncertainties are calculated in the same way as the “IAC” analysis above.

##### 3.1.3. Final Stellar Parameters

We determined the mean values for  $T_{\text{eff}}$ ,  $\log(g)$ ,  $[\text{Fe}/\text{H}]$ , and  $v_{\text{micro}}$  by combining the results from the IAC and BPG analyses via a mean, weighted by the inverse of the internal variances. For each parameter, we add in quadrature a systematic error of 18 K, 0.08, 0.03, and 0.02  $\text{km s}^{-1}$  for  $T_{\text{eff}}$ ,  $\log(g)$ ,  $[\text{Fe}/\text{H}]$ , and  $v_{\text{micro}}$ , respectively. These systematic errors are calculated based on the weighted standard deviation of the weighted means of each parameter using 18 spectra of 13 stars (seven MARVELS targets and six stars with well-known atmospheric parameters). These stars span  $T_{\text{eff}}$  from 5200–6500 K,  $\log(g)$  from 4.0 to 4.7,  $[\text{Fe}/\text{H}]$  from  $-0.5$  to  $+0.5$  and  $v_{\text{micro}}$  from 0.3 to 1.8  $\text{km s}^{-1}$ . The final stellar parameters are  $T_{\text{eff}} = 5879 \pm 29 \text{ K}$ ,  $\log(g) = 4.48 \pm$

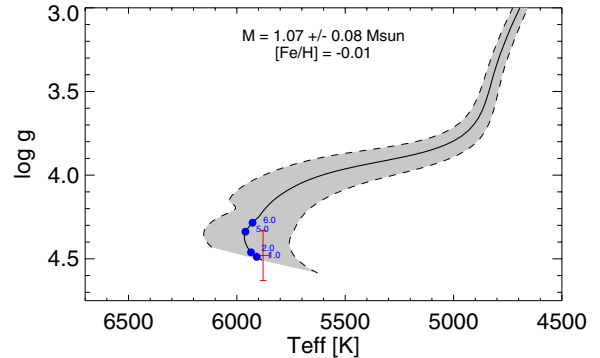


**Figure 1.** Top: the observed near UV through IR SED for TYC 4110-01037-1 is shown along with a best-fit NextGen model atmosphere. The resultant fundamental stellar parameters from this fit agreed to within  $1\sigma$  with the stellar parameters determined from analysis of moderate resolution spectra (Section 3.1). Bottom: by constraining  $T_{\text{eff}}$  and  $\log(g)$  to the spectroscopically determined values during the SED fit, we are able to better constrain the total line-of-sight extinction to be  $A_V = 0.16 \pm 0.04$ . Using this  $A_V$ , we estimate the distance to TYC 4110-01037-1 to be  $125.1 \pm 4.6$  pc.

(A color version of this figure is available in the online journal.)

$0.15$ ,  $[\text{Fe}/\text{H}] = -0.01 \pm 0.05$ , and  $v_{\text{micro}} = 0.94 \pm 0.04 \text{ km s}^{-1}$  (Table 2).

To check these parameters using a different observational technique, we constructed a spectral energy distribution (SED) for TYC 4110, using the near UV to Two Micron All Sky Survey (Cutri et al. 2003) and *WISE* (Wright et al. 2010) IR photometry compiled in Table 2 (see Figure 1). These data were fit with a NextGen model atmosphere (Hauschildt et al. 1999), and we limited the maximum line-of-sight extinction to be  $A_V < 0.28$  from analysis of dust maps from Schlegel et al. (1998). The resultant parameters,  $T_{\text{eff}} = 6000 \pm 200 \text{ K}$ ,  $\log g = 4.0 \pm 1.0$ ,  $[\text{Fe}/\text{H}] = 0.0 \pm 0.3$ , and  $A_V = 0.20 \pm 0.08$ , all agree to within  $1\sigma$  of the results found via analysis of our moderate resolution spectroscopy. We also fit these SED data by constraining the  $T_{\text{eff}}$  and  $\log g$  values to those derived from our spectroscopic analysis. The resultant fit (reduced  $\chi^2 = 2.62$ ; see panel (b) of Figure 1) provides a more robust estimate of  $A_V$ ,  $0.16 \pm 0.04$ . Using this total extinction estimate, and adopting a  $BC_V$



**Figure 2.** Observed stellar parameters for TYC 4110-01037-1 (red data) are compared to a Yonsei-Yale stellar (Demarque et al. 2004) evolutionary track for an  $M_\star = 1.07 M_\odot$  star with  $[\text{Fe}/\text{H}] = -0.01$ . Ages of 1.0, 2.0, 5.0, and 6.0 are indicated in blue, and  $1\sigma$  deviations in the evolutionary track are shown in the shaded region.

(A color version of this figure is available in the online journal.)

of  $-0.19 \pm 0.02$  (Cox 2000), we estimate the distance to TYC 4110 to be  $125.1 \pm 4.6$  pc (Table 2).

### 3.2. Stellar Mass and Radius

Using the spectroscopically determined values of  $T_{\text{eff}}$ ,  $\log g$ , and  $[\text{Fe}/\text{H}]$  (Table 2), we determined the mass and radius of TYC 4110 using the empirical Torres et al. (2010) relationship. We find  $M_\star = 1.07 \pm 0.08 M_\odot$  and  $R_\star = 0.99 \pm 0.18 R_\odot$  (Table 2). Our quoted errors include contributions from the uncertainties in our fundamental stellar parameters, as well as the scatter in the Torres et al. (2010) relationship ( $\sigma_{\log m} = 0.027$  and  $\sigma_{\log r} = 0.014$ ) and correlations of the best-fit coefficients from Torres et al. (2010) added in quadrature. We did not include covariances between  $T_{\text{eff}}$ ,  $\log g$ , and  $[\text{Fe}/\text{H}]$  in this error analysis; however, our final quoted uncertainties for these values do include a systematic error term that conservatively encapsulates any covariance between these parameters. We did however perform a Monte Carlo simulation of our spectroscopically determined stellar parameters and the Torres et al. (2010) relations, and found a stellar mass and radius consistent with the aforementioned values.

### 3.3. Evolutionary State

We assess the evolutionary state of TYC 4110 by comparing its spectroscopically measured fundamental stellar parameters against a Yonsei-Yale stellar evolutionary track (Demarque et al. 2004) for an  $M_\star = 1.07 M_\odot$  star having  $[\text{Fe}/\text{H}] = -0.01$ . This is done in Figure 2, where the shaded region depicts deviations in the evolutionary track which would be expected from a  $1\sigma$  ( $0.08 M_\odot$ ) change in the assumed stellar mass, while circles denote different time stamps in the track. TYC 4110 lies near a predicted age of  $\lesssim 5$  Gyr in Figure 2; we therefore conclude that it is a main-sequence dwarf star. The lack of any detectable Ca II *H* and *K* emission in our ARCES spectra ( $\log(R_{HK'}) \sim -5.1$ ) indicates the star is relatively inactive, and thus qualitatively consistent with the evolutionary state we derive.

### 3.4. Systemic and Rotational Velocity

We computed the absolute RV of TYC 4110 by cross-correlating the six epochs of SARG spectra against a solar spectrum. After removing the RV contribution at each epoch induced by the presence of TYC 4110's companion (Table 1), we determine the systemic velocity of TYC 4110,  $v_{\text{systemic}}$ , to

be  $25.9 \pm 0.2 \text{ km s}^{-1}$  (Table 2). We also compared these SARG data to broadened versions of Kurucz ATLAS synthetic spectra to constrain the rotational velocity,  $v_{\text{rot}} \sin i$ , of TYC 4110. After considering a range of macroturbulence values, we find  $v_{\text{rot}} \sin i \lesssim 3 \text{ km s}^{-1}$ , which is slightly below the level of instrumental broadening present in these data ( $\sim 5.3 \text{ km s}^{-1}$ ).

#### 4. TYC 4110-01037-1’S COMPANION

##### 4.1. Binary Companion Detection

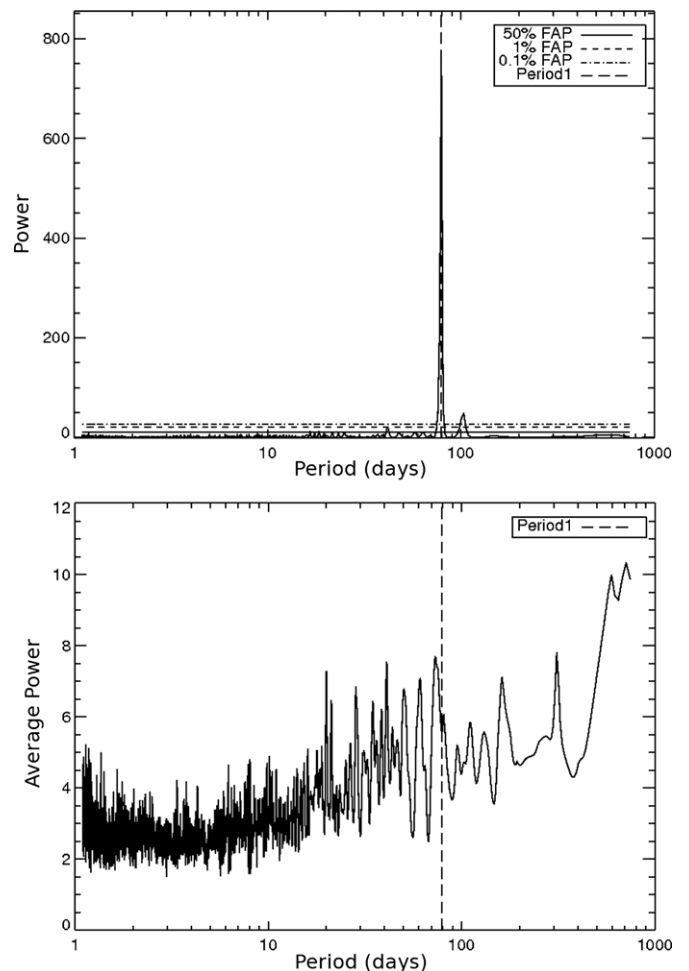
Analysis of post-pipeline processed MARVELS data involves searching for periodic behavior which is consistent with Keplerian orbital motion and filtering out “contaminant” RV signals which do not arise from the presence of a companion. One of the first steps in this process is to compute a Lomb–Scargle (LS) periodogram (Lomb 1976; Scargle 1982) and search for periodic signals which significantly exceed a conservative false alarm probability assessment. There have been several implementations of this method (Press & Rybicki 1989); we followed Cumming (2004) which uses the comparison of the  $\chi^2$  values between a sinusoidal fit at a given frequency and a fit to the mean to generate the power term (see, e.g., Cumming’s Equation (2)). This form was chosen to be fully extensible by adding linear terms, harmonic terms, or even a fully Keplerian fit. We stepped through frequency space using steps and a search window as appropriate for our data sampling, as described in Press et al. (1992). In order to interpret the significance of this power spectrum, false alarm probabilities were calculated using the techniques in Baluev (2008).

Data from the current MARVELS pipeline have systematic effects present which can mimic a companion signal. We can significantly mitigate this issue by taking advantage of the fact that the MARVELS instrument observes 60 stars at a time. As a result, we can search for periodic signals from all stars on a given plate and use any detected signals to characterize systematics in our data. This is done by taking the sum of the power for each frequency across the entire plate. We then remove the highest power from each frequency (so that actual companions do not skew the average), excluding any power associated with the candidate companion, and compute the average.

Figure 3 indicates TYC 4110 exhibits a strong  $\sim 79$  day period signal. The companion to TYC 4110, hereafter referred to as MARVELS-3B, does not match any strong periodic signature identified in the power spectrum of all stars located on the same SDSS-III plate (bottom panel; Figure 3), and is therefore not caused by any known systematic artifact in our instrument or reduction pipeline.

##### 4.2. Radial Velocity Fits

Radial velocities derived from MARVELS and SARG data were fit with the EXOFAST code (J. Eastman et al. 2012, in preparation) to extract detailed Keplerian orbital parameters. We first performed an independent fit of the MARVELS data and re-scaled the MARVELS error bars to force the probability of  $\chi^2$ ,  $P(\chi^2)$ , = 0.5. Since we did not have enough SARG data points to perform an independent fit solely on these data, we then fit the combined (MARVELS + SARG) data, and re-scaled the SARG errors to force  $P(\chi^2) = 0.5$ . The fitting of the combined data set and re-scaling of the SARG errors were iterated until a convergent solution was achieved. The MARVELS and (MARVELS + SARG) data yielded consistent results to within  $1\sigma$  of the fit errors. We also computed the  $\chi^2$  of the SARG data about the MARVELS-only fit, and the resultant

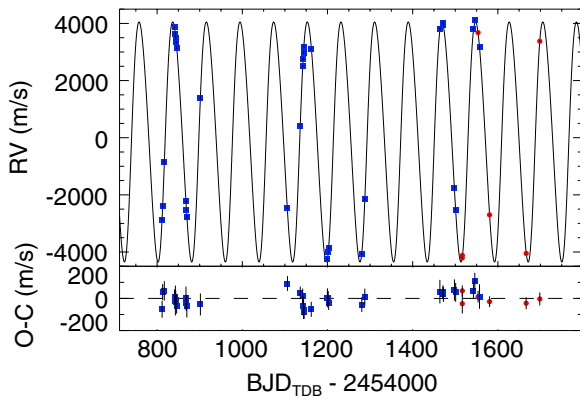


**Figure 3.** Periodogram for RV measurements of TYC 4110-01037-1 (panel a) indicates the strong presence of a  $\sim 79$  day periodic signature, indicated by the dashed vertical line. This signal is not seen to coincide with any strong feature in the periodogram for all stars located on the same SDSS-III plate as this object (panel b), indicating it is not caused by a known artifact of our instrument or reduction pipeline.

value ( $\chi^2 = 8.47$  for 5 degrees of freedom) indicates such a fit would only happen by chance  $\sim 13\%$  of the time. We hereafter only consider the combined MARVELS + SARG fit.

The raw MARVELS and SARG radial velocities were computed on independent, relative scales. We determined that the best offsets to simultaneously analyze these data about a zero point of  $0 \text{ m s}^{-1}$  were  $1345 \pm 24 \text{ m s}^{-1}$  (SARG) and  $8583 \pm 12 \text{ m s}^{-1}$  (MARVELS); the RVs quoted in Table 1 have had these offsets applied. The RV errors listed in Table 1 include the re-scaling factors described above. The inclusion of an additional linear term was explored in the fitting process, but there is no compelling evidence for an acceleration due to another companion, with a best-fit linear slope of  $0.096^{+0.039}_{-0.040} \text{ m s}^{-1} \text{ day}^{-1}$  observed, corresponding to a  $2.4\sigma$  deviation.

As seen in the full RV curve (Figure 4) and in the phase-folded curve (Figure 5), these data are described by a  $78.994 \pm 0.012$  day period, a moderately elliptical ( $e = 0.1095 \pm 0.0023$ ) orbit, and a semi-amplitude  $K = 4199 \pm 11 \text{ m/s}$ . Full fit parameters for TYC 4110 are presented in Table 3. To search for evidence that MARVELS-3B was a transiting system, we computed an LS periodogram of the available SuperWASP photometry, but found no evidence of variability at the  $\sim 79$  day period of MARVELS-3B above a level of  $\sim 0.8\%$ .



**Figure 4.** Derived relative radial velocities from the MARVELS (blue squares) and SARG (red circles) spectrographs are overlaid with the best-fit orbital solution described in Section 4 and compiled in Table 3. Residuals to this fit are shown in the bottom panel.

(A color version of this figure is available in the online journal.)

**Table 3**  
Properties of MARVELS-3B

Parameter	Value
$T_C$ (BJD <sub>TDB</sub> −2,450,000)	$5175.97 \pm 0.14$
$P$ (days)	$78.994 \pm 0.012$
$e$	$0.1095 \pm 0.0023$
$\omega$ (radians)	$4.380^{+0.041}_{-0.042}$
$K$ (m s <sup>−1</sup> )	$4199 \pm 11$
$\gamma_{\text{TNG}}$ (m s <sup>−1</sup> )	$1338 \pm 19$
$\gamma_{\text{APO}}$ (m s <sup>−1</sup> )	$2945.0^{+10.0}_{-9.9}$
$e \cos(\omega)$	$-0.0357^{+0.0042}_{-0.0043}$
$e \sin(\omega)$	$-0.1034 \pm 0.0027$
$T_P$ (BJD <sub>TDB</sub> −2,450,000)	$5210.32^{+0.50}_{-0.51}$
$a$ (sin $i = 1$ )	$0.38 \text{ AU}$
$M$ ( $M_{\text{Jup}}$ )	$>97.7 \pm 5.8$

**Notes.** A summary of some of the basic orbital properties of MARVELS-3B. The quoted minimum mass corresponds to the limiting case of  $\sin i = 1$ . Note that  $T_P$  corresponds to the time of periastron while  $T_C$  corresponds to the time of conjunction.

We determined the mass for MARVELS-3B using

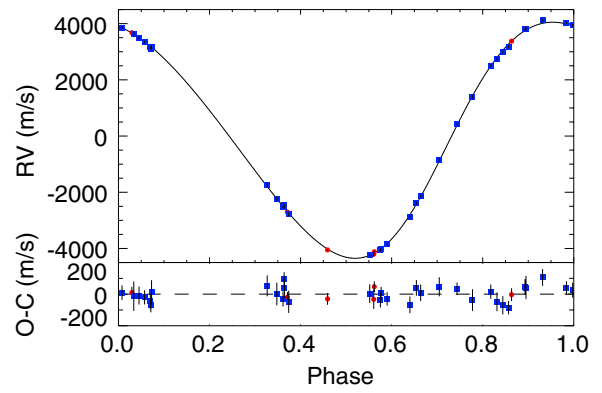
$$\frac{(M_c \sin i)^3}{(M_* + M_c)^2} = \frac{K^3 (1 - e^2)^{3/2} P}{2\pi G} \quad (2)$$

$$\frac{(M_c \sin i)^3}{(M_* + M_c)^2} = (5.953 \pm 0.047) \cdot 10^{-4} M_\odot \quad (3)$$

and the fit parameters compiled in Table 3. This yields a minimum companion mass (if  $\sin i = 1$ ) of  $97.7 \pm 5.8 M_{\text{Jup}}$ , which places MARVELS-3B slightly above the generally accepted BD upper mass limit of  $80 M_{\text{Jup}}$  and into the low-mass star regime. The minimum mass ratio,  $q$ , of the companion to the primary is  $0.087 \pm 0.003$ .

### 4.3. Binary Companion Mass

The true mass of the companion depends on the inclination  $i$  of the orbit, which is unknown. However, we can estimate the posterior probability distribution of the true companion mass, given an isotropic distribution of orbits, and adopting a prior for the distribution of the companion mass ratios. We proceed to do this using a Monte Carlo method, following the methodology described in detail in Fleming et al. (2010)



**Figure 5.** Phase-folded radial velocity curve is shown, for a MARVELS-3B period of  $78.994 \pm 0.012$  days and eccentricity of  $0.1095 \pm 0.0023$ . Based on the derived stellar mass of  $1.07^{+0.08}_{-0.08} M_\odot$  (Table 2), we determine the minimum (sin  $i = 1$ ) mass of MARVELS-3B to be  $>97.7 \pm 5.8 M_{\text{Jup}}$ .

(A color version of this figure is available in the online journal.)

and Lee et al. (2011), which we briefly summarize here. We combine the posterior distribution of orbital parameters  $K$ ,  $e$ , and  $P$  obtained from the Markov Chain Monte Carlo (MCMC) fit to the RV data, with an estimate of the joint distribution of the primary mass and radius obtained using the spectroscopically determined  $T_{\text{eff}}$ ,  $\log g$ , and  $[\text{Fe}/\text{H}]$  combined with the Torres et al. (2010) relations, accounting for all sources of uncertainty in the measured values and the relations themselves. We draw values of  $\cos i$  from a uniform distribution. The values of  $K$ ,  $e$ , and  $P$  determine the mass function  $(M_c \sin i)^3 / (M_* + M_c)^2$ , and then the value of  $i$  along with the primary mass  $M_*$  determines  $M_c$ . Finally, we appropriately weight the resulting distribution of  $M_c$  by our prior on the mass ratio  $q$ .

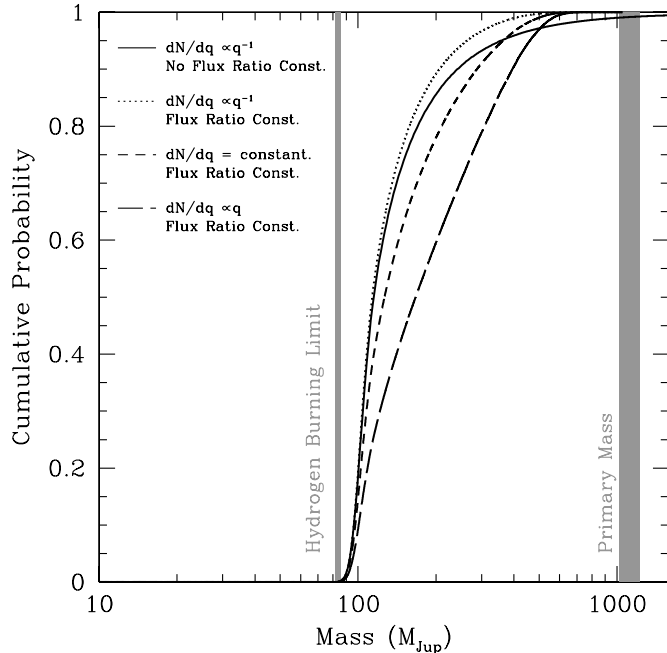
As described in Section 1, the mass ratio of companions around G dwarfs is not well constrained by current observations and MARVELS-3B likely lies in a relatively underpopulated region of mass ratio parameter space. Nevertheless, we consider several different priors on the companion mass ratio which we suggest are reasonable given current observations (see, e.g., Grether & Lineweaver 2006) of the form:  $dN/dq \propto q^{+1}$ ,  $dN/dq \propto q^{-1}$ , and  $dN/dq = \text{constant}$ . We note that massive companions are ruled out by the lack of a statistically significant infrared excess in the SED (Figure 1) and the lack of a secondary component in our high-resolution optical spectra (see discussion below). We include this constraint by weighting the resulting distribution of  $M_c$  by  $\exp[-0.5(\Delta K/\Delta K_{\text{max}})^2]$ , where  $\Delta K_{\text{max}}$  is the upper limit on the excess flux (in magnitudes) in the  $K$  band, and  $\Delta K$  is the excess flux contributed by a companion of mass  $M_c$  and a primary of mass  $M_*$ , as determined using the Baraffe et al. (1998) solar metallicity,  $Y = 0.275$ , 1 Gyr mass–magnitude relations (note that we could have adopted any isochrone in the range of 1–10 Gyr with negligible difference). We caution the reader that this specific constraint does not fully and uniformly represent the prior for every possible configuration of the companion, but rather is a reasonable, simplifying set of conditions. We did not observe a statistically significant IR excess flux in TYC 4110’s SED (Figure 1); thus, we used the  $3\sigma$  standard deviation (0.06 mag) of the  $K_s$ -band data for  $\Delta K_{\text{max}}$ . We note that the IR flux contribution from the wider separation candidate tertiary companion, discussed in more detail in Section 4.4, is less than this  $\Delta K_{\text{max}}$  and therefore does not influence our mass estimate.

The resultant cumulative distributions of the true mass are shown in Figure 6, and we summarize the median mass for each

**Table 4**  
MCMC Properties of MARVELS-3B

Assumed Prior	Mass of MARVELS-3B	Transit Probability	$q$ (Mass Ratio)
None ( $\sin i = 1$ )	97.7 $M_{\text{Jup}}$	1	$>0.087 \pm 0.003$
$dN/dq \propto q^{+1}$	166.2 $M_{\text{Jup}}$	0.0055	0.149
$dN/dq \propto q^{-1}$	113.0 $M_{\text{Jup}}$	0.0129	0.100
$dN/dq = \text{const}$	125.9 $M_{\text{Jup}}$	0.0092	0.112

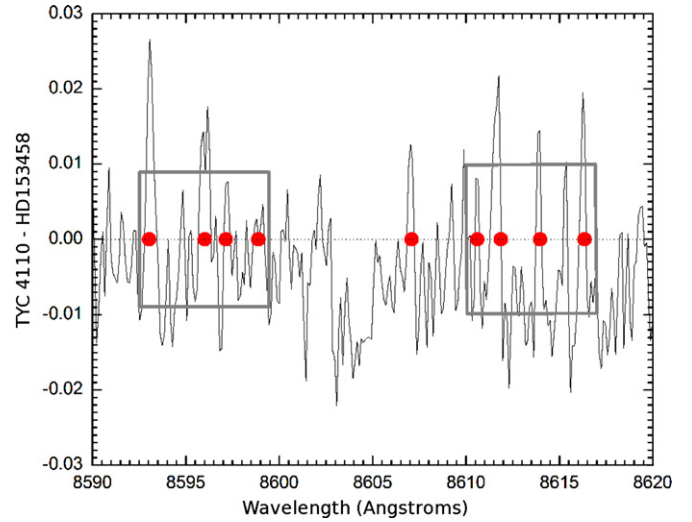
**Notes.** A summary different mass estimates of MARVELS-3B and the resultant mass ratio for different assumed priors on the statistical companion mass ratio around G dwarfs and our MCMC analysis. The prior “none” corresponds to the minimum mass of MARVELS-3B, simply assuming  $\sin i = 1$ . For all other priors, the quoted companion mass and  $q$  values are the median mass determined from our MCMC analysis described in Section 4 and shown in Figure 6.



**Figure 6.** Cumulative probability that the mass of MARVELS-3B is less than a given mass is shown, for four different priors on the companion mass ratio described in Section 4.

of these priors, along with the resultant mass ratio, in Table 4. Since these probabilistic median values rely on the simplifying assumptions we have made, we have not assigned formal confidence limits to these values, to prevent overinterpretation of their robustness. For each prior, we note that the resultant median mass is in the M dwarf region with a low ( $<0.2$ ) mass ratio, and companions more massive than  $0.5 M_{\odot}$  are ruled out at the 95% probability level.

Finally, we also analyzed the ARCES spectrum of TYC 4110, obtained at a phase of  $\sim 0.71$ , to search for evidence of MARVELS-3B. We first note that we detected no evidence that the system was an SB2, which suggests  $q \lesssim 0.65$  (Halbwachs et al. 2003), i.e., MARVELS-3B is less massive than a mid K-type dwarf. Figure 7 illustrates the red optical difference spectrum computed by subtracting the spectrum of a G dwarf with very similar fundamental stellar parameters, HD 153458, from TYC 4110. Both the known binary companion to TYC 4110 (MARVELS-3B) and the candidate tertiary companion (see Section 4.4) could fill in the spectral features identified with red dots in Figure 7, leading to positive deviations in the difference spectrum, although differentiating the precise amount of any contribution from the secondary versus the candidate tertiary is not possible. While calibrating our



**Figure 7.** Continuum normalized spectrum of HD153458 was subtracted from the continuum normalized spectrum of TYC 4110-01037-1. The  $1\sigma$  Poisson errors in the data are illustrated with gray boxes. As discussed in Section 4.3, we note that minor mismatches between the properties of the reference and science spectra could produce noticeable subtraction residuals in line wings, which suggests that only strong, repeatable deviations in these difference spectra should be interpreted as real contributions from companion(s). An M3-type companion would have contributed a 2% flux enhancement to the system. However, the difference spectrum does not exhibit  $>3\sigma$  deviations above the level of the Poisson noise (0.8%) and continuum normalization uncertainties present in the data, which sets the lower mass limit for MARVELS-3B that can be ascertained from these specific data.

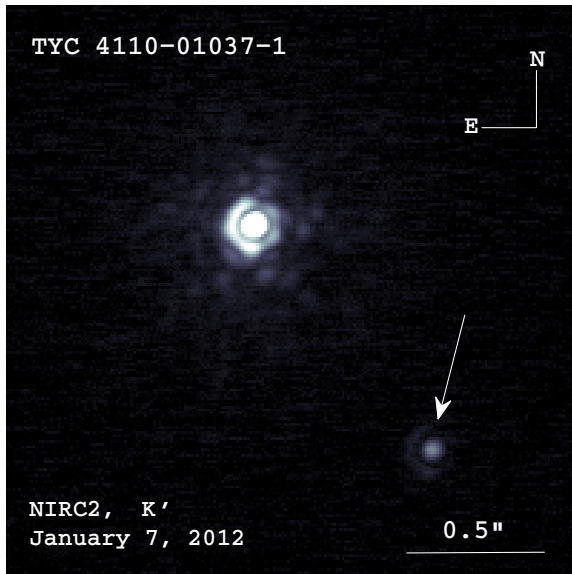
(A color version of this figure is available in the online journal.)

usage of this technique, we found that minor mismatches between the properties of the reference and science spectra could produce noticeable subtraction residuals in line wings (as seen in Figure 7), which suggests that only strong, repeatable deviations in these difference spectra should be interpreted as real contributions from companion(s). Using spectra from the Pickles (1998) library, we estimate that a M3-type companion would have contributed a  $\sim 2\%$  flux enhancement to the system. The difference spectrum does not exhibit  $>3\sigma$  deviations above the level of the Poisson noise (0.8%) and continuum normalization uncertainties present in the data, which sets the lower mass limit for MARVELS-3B that can be ascertained from these specific data.

#### 4.4. Candidate Tertiary Companion

Triple star systems are a relatively common outcome of the star formation process (see, e.g., Tokovinin 2004). To further assess the multiplicity of TYC 4110, we acquired adaptive optics images on 2012 January 7 using NIRC2 (PI: Keith Matthews) at





**Figure 8.** Keck adaptive optics image of TYC 4110-01037-1 in  $K'$ . We have detected a faint candidate tertiary companion (indicated by the arrow) with red colors that is separated by  $986 \pm 4$  mas from the primary star. If it is physically associated with the primary, it is most likely a dM3–dM4 star.

(A color version of this figure is available in the online journal.)

the Keck Observatory in natural guide star mode. Our initial data set consisted of nine dithered images taken in the  $K'$  filter. Inspection of the raw frames showed evidence for a faint candidate companion located to the southwest of TYC 4110. Figure 8 shows the fully processed  $K'$  image.

We measured an accurate position for the candidate companion using the technique described in Crepp et al. (2012). We first fit Gaussian functions to the stellar and companion point-spread functions to locate their centroids in each frame. The primary star was not saturated in any of our dithered images. We then correct for distortion in the NIRC2 focal plane (narrow camera mode) using the publicly available software provided by the Keck Observatory astrometry support page.<sup>22</sup> The results are averaged and the uncertainty in the separation and position angle is taken as the standard deviation, taking into account uncertainty in the plate scale and orientation of the array by propagating these errors to the final calculated position. Adopting a plate scale of  $9.963 \pm 0.006$  mas pixel<sup>-1</sup> and instrument orientation relative to the sky of  $0^\circ:13 \pm 0^\circ:02$ , as measured by Ghez et al. (2008), we find a companion separation and position angle of  $\rho = 986 \pm 4$  mas and P.A. =  $218^\circ:1 \pm 0^\circ:3$ , respectively.

Upon noticing the companion, we obtained additional images in the  $J$  and  $H$  bands to facilitate characterization. Our aperture photometry indicates that the object has red colors:  $\Delta J = 4.219 \pm 0.104$ ,  $\Delta H = 3.940 \pm 0.032$ , and  $\Delta K' = 3.805 \pm 0.027$  mag. Table 5 lists its apparent magnitude as measured relative to the primary star, taking into account the combined light from each source.

Both the  $(J - H) = 0.55$  and  $(J - K') = 0.75$  colors indicate a spectral type of  $\sim$ M3V (Leggett et al. 2002). Assuming the candidate is situated at the same distance as the primary, we find that the absolute magnitudes,  $M_J = 8.10 \pm 0.21$ ,  $M_H = 7.55 \pm 0.32$ ,  $M_K = 7.36 \pm 0.13$ , are each consistent with an  $\sim 0.25 M_\odot$  star when compared to the Girardi et al. (2002)

**Table 5**

Properties of the Candidate Tertiary Companion to TYC 4110-01037-1

Filter	Magnitude
$J$	$13.59 \pm 0.13$
$H$	$13.04 \pm 0.24$
$K'$	$12.84 \pm 0.05$

**Note.** The computed apparent magnitude of the candidate tertiary companion to TYC 4110 detected in Figure 8 is compiled.

evolutionary models, which corresponds to a main-sequence spectral type of  $\sim$ dM4. The relations from Table 5 of Kraus & Hillenbrand (2007) yield the same result (dM4), though with a possibly lower mass estimate of  $\sim 0.20 M_\odot$ .

Given the R.A., decl., and distance of TYC 4110, the a priori likelihood of detecting a background star within  $1''0$  is  $\sim 0.8\%$ . With a proper motion of  $[-0.20, -99.40]$  mas yr<sup>-1</sup>, a time baseline of several months will be sufficient to assess its association with the primary star. We note that the detection and mass constraints placed on MARVELS-3B in this paper hold regardless of whether or not this candidate tertiary companion is confirmed to be comoving with the primary star.

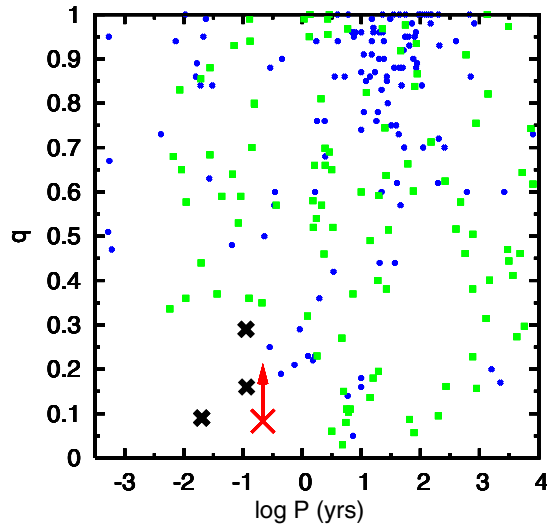
## 5. DISCUSSION

We discuss some of the derived properties for MARVELS-3B in the context of previous studies of low-mass companions to solar-like stars. Both Duquennoy & Mayor (1991) and Raghavan et al. (2010) demonstrate that companions to solar-like stars having orbital periods  $\leq 12$  days are circular; however, companions having orbital periods similar to that of MARVELS-3B,  $\sim 79$  days, exhibit eccentricities from 0 to 0.6 (Duquennoy & Mayor 1991; Mayor et al. 1992; Raghavan et al. 2010). MARVELS-3B’s modest eccentricity of  $\sim 0.11$  therefore is clearly consistent with that observed for other similar period companions.

Arguably the most distinctive feature of TYC 4110 is its extremely low mass ratio,  $q$ , of  $\geq 0.087 \pm 0.003$ , given its relatively short  $\sim 79$  day period. As illustrated in Figure 9, previous statistical investigations of binarity in solar-like ( $T_{\text{eff}} \lesssim 6000$  K) stars have found evidence that the short period BD desert extends in mass toward the low-mass star regime (Burgasser et al. 2007; Bouchy et al. 2011; Sahlmann et al. 2011). A similar desert of short period, low  $q$  companions to low-mass K and M dwarf stars has also been observed (Figure 9; see also Burgasser et al. 2007). The studies of companions around solar-like stars by both Duquennoy & Mayor (1991) and Raghavan et al. (2010) report no firm detection of low  $q$  binary companions with orbital periods  $< 100$  days. The closest short period analog observed by Raghavan et al. (2010; see, e.g., their Figure 17) is a multiple ( $> 2$  components)  $q \sim 0.23$  system with an orbital period of  $\sim 50$  days, while the closest short period binary is a  $\sim 1$  day period object with a  $q$  of  $\sim 0.4$ . All other low  $q$  binaries in their sample have orbital periods  $\geq 5000$  days. Mayor et al. (2001) also report a sparse number of low  $q$  binary companions to solar-like stars, but do not quantify the orbital periods of these objects.

The absolute “dryness” of the low-mass ratio, short-period desert for solar-like ( $T_{\text{eff}} \lesssim 6000$  K) illustrated in Figure 9 is a subject of active investigation and debate in the literature. OGLE-TR-122b (Pont et al. 2005), Kepler-16b (Doyle et al. 2011), and vB 69 (Bender & Simon 2008) are short period, low  $q$ ,

<sup>22</sup> [http://www2.keck.hawaii.edu/inst/nirc2/forReDoc/post\\_observing/dewarp/](http://www2.keck.hawaii.edu/inst/nirc2/forReDoc/post_observing/dewarp/)



**Figure 9.** Mass ratio,  $q$ , versus orbital period distribution of binary stars having periods  $< 10,000$  years and primary star  $T_{\text{eff}} \lesssim 6000$  K is shown. Filled blue circles represent K and M dwarf primary stars and is based on data compiled in literature (Halbwachs et al. 2003; Maceroni & Montalban 2004; Burgasser et al. 2007; Becker et al. 2008; Bender & Simon 2008; Rucinski & Pribulla 2008; Dimitrov & Kjurkchieva 2010; J. R. A. Davenport et al. 2012, in preparation) and at <http://www.vlmbinaries.org>. Among these low-mass stars, a distinct lack of low  $q$  binaries at short orbital periods is present. A similar trend is also observed in the distribution of confirmed binaries around solar-like ( $0.8 M_{\odot} < M < 1.1 M_{\odot}$ ) stars (filled green squares), as seen in data reproduced from tabulated data in literature (Halbwachs et al. 2003; Bender & Simon 2008; Raghavan et al. 2010; Sahlmann et al. 2011). The mass ratio of the TYC 4110 (large red cross and an arrow of arbitrary size), OGLE-TR-122 (small black cross; adopted from Pont et al. 2005), Kepler-16 (small black cross; adopted from Doyle et al. 2011), and vB 69 (small black cross; adopted from Bender & Simon 2008) systems are unique in that they lie within this mass-ratio–period deficit.

(A color version of this figure is available in the online journal.)

solar-like binary systems that populate this parameter space. The statistical frequency of objects like OGLE-TR-122b and Kepler-16b have not been quantified by the OGLE or Kepler surveys; hence, it is plausible that they are indeed rare. We note that there have been suggestions the mass ratios of binary companions surrounding F7 to K-type stars are more broadly distributed and that no clear low-mass ratio desert exists (see Figure 8 in Halbwachs et al. 2003). However, we have included all of the companions surrounding G-type ( $0.8 M_{\odot} < M < 1.1 M_{\odot}$ ) and K- and M-type primaries tabulated in Halbwachs et al. (2003) (but omitting data from their survey which was not tabulated in print or online) in Figure 9, and still clearly see a short period, low-mass ratio companion deficit. Clearly, additional observational studies which precisely characterize the stellar properties of the host star and characterize the properties of their binary companions are needed to perform an accurate meta-analysis of the dependence of companion mass ratios as a function of orbital period and host star mass. These studies should make careful note of their observational biases to facilitate a more robust cross-correlation of results compiled from different surveys. A future meta-analysis would also particularly benefit from having current and future studies fully tabulating the fundamental properties of the binary systems they investigate.

As noted in Section 1, short-period, low  $q$  companions have been reported around stars slightly more massive than the Sun (F-type stars; Bouchy et al. 2005; Pont et al. 2006; Beatty et al. 2007; Bouchy et al. 2011). Bouchy et al. (2011) propose that

short-period low  $q$  companions might form around a wide mass range of stars, including G-type stars, but suggest that weaker magnetic disk braking during the early formation history of F-type stars might transfer less angular momentum to their companion bodies, thereby preventing catastrophic decays of their orbits. Conversely, Bouchy et al. (2011) propose that a stronger disk braking in young G-type stars might distribute more angular momentum to their companion bodies, causing (initially) short period companions to migrate inward and become engulfed by the primary. While intriguing, this proposed evolutionary scenario would clearly benefit by a more robust assessment of how “dry” the short-period, low  $q$  desert is around GKM dwarfs as compared to F dwarfs.

The precise mass ratio of MARVELS-3B is not known due to the unknown inclination of the system, thus our observations only set a lower limit of  $q$  of  $> 0.087 \pm 0.003$ . However, as demonstrated in Section 4, our Bayesian analysis of the system using four plausible prior assumptions all indicate the likely median mass of MARVELS-3B is a dM star, yielding mass ratios of  $0.087 < q < 0.149$  (Figure 6 and Table 4). Like OGLE-TR-122b (Pont et al. 2005) and Kepler-16b (Doyle et al. 2011), MARVELS-3B therefore seems likely to be an outlier to the mass-ratio–period relationships commonly observed for both solar-like stars and lower-mass dM stars (Figure 9).

In this context, we note that analyses of the period distribution of exoplanets have revealed a deficit of such bodies having orbital periods of 10–100 days, aka the “period valley” (Udry et al. 2003; Jones et al. 2003). Wittenmyer et al. (2010) suggest that this observed deficit is real for the giant planet population ( $M > 100 M_{\oplus}$ ), but that any deficit of lower mass planets ( $10\text{--}100 M_{\oplus}$ ) in this period regime might be the result of selection effects. One possible explanation for the dearth of giant planets in 10–100 day orbits is a decrease in the amount of orbital migration which such objects experience (see, e.g., Trilling et al. 1998).

Migration could also play a role in setting the observed period distribution of the low-mass stellar binary regime. The orbital evolution of binaries has been explored computationally, and stellar accretion, the interaction between binaries with their natal gas disks, and interactions between triple components can influence these systems (see, e.g., Bate et al. 2002; Stamatellos & Whitworth 2009; Kratter 2011). Bate et al. (2002), for example, found such processes were successful at producing short-period binaries in high-mass ratio systems ( $q \geq 0.3$ ), but it is uncertain as to whether these specific simulations could produce short-period, low  $q$  systems like MARVELS-3B.

$N$ -body simulations of the early evolution of stellar clusters which include instantaneous gas removal (Moeckel & Bate 2010) are beginning to better reproduce the number of unequal mass solar-like binaries observed (Duquennoy & Mayor 1991; Raghavan et al. 2010). Potentially relevant for MARVELS-3B, Moeckel & Bate (2010) showed that one simulated triple system comprised of a 0.96 and 0.73  $M_{\odot}$ , 2 AU separation binary with a 0.21  $M_{\odot}$  tertiary at 12 AU, broke up into a tight (0.1 AU separation) binary system comprised of the 0.21 and 0.73  $M_{\odot}$  components (e.g., a mass ratio,  $q$ , of 0.29). We therefore speculate that it is possible that the short period, low  $q$  MARVELS-3B binary was initially part of a tertiary (or larger) system with much different initial orbital parameters and only achieved its final orbital configuration following the dispersal of the cluster in which it formed. Although our analysis of available SuperWASP photometry and MARVELS+SARG RV data exhibited no evidence of the presence of additional, long-period ( $\geq 2$  years) bodies in

the system, our single-epoch detection of a candidate tertiary body in the system via high contrast imaging could support this interpretation. Additional epochs of imagery should be pursued to establish if this body is comoving with the TYC 4110 system. Although beyond the scope of this paper, future simulations of binary migration and orbital evolution during cluster dispersal should explore the limits and frequency at which they can reproduce short-period, low-mass ratio binaries for solar-like stars.

## 6. CONCLUSIONS

We present a detailed analysis of the fundamental properties of the solar-like star TYC 4110-01037-1 and its very low mass stellar companion. This analysis was performed in the context of our long-term goal of performing a detailed statistical analysis of global trends in the population of well vetted and characterized BDs and low-mass binary companions identified by the MARVELS survey. We find:

1. TYC 4110-01037-1 is a  $\lesssim 5$  Gyr solar-like star characterized by  $T_{\text{eff}} = 5879 \pm 29$  K,  $\log g = 4.48 \pm 0.15$ , and  $[\text{Fe}/\text{H}] = -0.01 \pm 0.05$ . We determine the stellar mass to be  $1.07 \pm 0.08 M_{\odot}$  and stellar radius to be  $0.99 \pm 0.18 R_{\odot}$ .
2. MARVELS-3B is a  $>97.7 \pm 5.8 M_{\text{Jup}} (M \sin i)$  companion to TYC 4110-01037-1, which follows a moderately elliptical ( $e = 0.1095 \pm 0.0023$ ),  $78,994 \pm 0.012$  day orbital period.
3. The mass ratio,  $q$ , of the companion to the primary is  $\geq 0.087 \pm 0.003$ . MARVELS-3B therefore resides in a short period, low  $q$  desert analogous to the short-period BD desert.
4. We speculate that MARVELS-3B might have initially formed in a tertiary system with much different orbital parameters and achieved its present-day configuration following the dispersal of the cluster in which it formed. A candidate tertiary body has been identified via single-epoch, high contrast imagery. If this object is confirmed to be comoving, we estimate it would be a dM4 star.

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